ISSN- 2350-0530(O), ISSN- 2394-3629(P) DOI: 10.29121/granthaalayah.v6.i8.2018.1260



# INTERNATIONAL JOURNAL OF RESEARCH GRANTHAALAYAH A knowledge Repository



थालयाः ५ १

## DECREASE OF REAL POWER LOSS BY ADAPTED ALGORITHM

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## Abstract

In this paper, Adapted Flower Pollination (AFP) algorithm is proposed to solve the optimal reactive power problem. Flower pollination algorithm has been improved by comprising of the elements of chaos theory, Shuffled frog leaping search and Levy Flight. In the AFP algorithm, the initial population is generated using the circle map, frog leaping local search is performed by each solution and when rand>p, modified Levy flight with integration of inertia weight in global pollination is performed on that particular solution. Proposed AFP algorithm has been tested in standard IEEE 57 bus test system and simulation results show clearly the better performance of the proposed algorithm in reducing the real power loss.

*Keywords:* Optimal Reactive Power; Transmission Loss; Flower Pollination Algorithm; Chaos Theory; Shuffled Frog Leaping Search and Levy Flight.

Cite This Article: Dr.K. Lenin (2018). "DECREASE OF REAL POWER LOSS BY ADAPTED ALGORITHM." International Journal of Research - Granthaalayah, 6(8), 41-50. https://doi.org/10.29121/granthaalayah.v6.i8.2018.1260.

## 1. Introduction

Optimal reactive power problem is to minimize the real power loss and bus voltage deviation. Various numerical methods like the gradient method [1-2], Newton method [3] and linear programming [4-7] have been adopted to solve the optimal reactive power dispatch problem. Both the gradient and Newton methods have the complexity in managing inequality constraints. If linear programming is applied then the input- output function has to be uttered as a set of linear functions which mostly lead to loss of accuracy. The problem of voltage stability and collapse play a major role in power system planning and operation [8]. Evolutionary algorithms such as genetic algorithm have been already proposed to solve the reactive power flow problem [9-11].

Evolutionary algorithm is a heuristic approach used for minimization problems by utilizing nonlinear and non-differentiable continuous space functions. In [12], Hybrid differential evolution algorithm is proposed to improve the voltage stability index. In [13] Biogeography Based algorithm is projected to solve the reactive power dispatch problem. In [14], a fuzzy based method is used to solve the optimal reactive power scheduling method. In [15], an improved evolutionary

programming is used to solve the optimal reactive power dispatch problem. In [16], the optimal reactive power flow problem is solved by integrating a genetic algorithm with a nonlinear interior point method. In [17], a pattern algorithm is used to solve ac-dc optimal reactive power flow model with the generator capability limits. In [18], F. Capitanescu proposes a two-step approach to evaluate Reactive power reserves with respect to operating constraints and voltage stability.

In [19], a programming based approach is used to solve the optimal reactive power dispatch problem. In [20], A. Kargarian et al present a probabilistic algorithm for optimal reactive power provision in hybrid electricity markets with uncertain loads. This paper proposes Adapted Flower Pollination (AFP) algorithm is proposed to solve the reactive power problem. The basic idea of flower pollination process which leads to the formulation of flower pollination algorithm (FPA) [21] is first introduced and subsequently, chaos theory, Shuffled frog leaping search and Levy Flight are introduced. Proposed AFP algorithm has been evaluated in standard IEEE 118 & practical 191 bus test systems. Simulation results show that our proposed approach outperforms all the entitled reported algorithms in minimization of real power loss.

## 2. Problem Formulation

#### **Active Power Loss**

The objective of the reactive power dispatch is to minimize the active power loss in the transmission network, which can be described as follows:

$$F = PL = \sum_{k \in Nbr} g_k \left( V_i^2 + V_j^2 - 2V_i V_j cos\theta_{ij} \right)$$
(1)

Where  $g_k$ : is the conductance of branch between nodes i and j, Nbr: is the total number of transmission lines in power systems.  $P_d$ : is the total active power demand,  $P_{gi}$ : is the generator active power of unit i, and  $P_{gsalck}$ : is the generator active power of slack bus.

## **Voltage Profile Improvement**

For minimizing the voltage deviation in PQ buses, the objective function becomes:

$$F = PL + \omega_v \times VD \tag{2}$$

Where  $\omega_v$ : is a weighting factor of voltage deviation.

VD is the voltage deviation given by:

$$VD = \sum_{i=1}^{Npq} |V_i - 1| \tag{3}$$

## **Equality Constraint**

The equality constraint of the problem is represented by the power balance equation, where the total power generation must cover the total power demand and the power losses:

$$P_G = P_D + P_L \tag{4}$$

This equation is solved by running Newton Raphson load flow method, by calculating the active power of slack bus to determine active power loss.

# **Inequality Constraints**

The inequality constraints reflect the limits on components in the power system as well as the limits created to ensure system security. Upper and lower bounds on the active power of slack bus, and reactive power of generators:

$$P_{gslack}^{min} \le P_{gslack} \le P_{gslack}^{max} \tag{5}$$

$$Q_{gi}^{min} \le Q_{gi} \le Q_{gi}^{max}, i \in N_g \tag{6}$$

Upper and lower bounds on the bus voltage magnitudes:

$$V_i^{min} \le V_i \le V_i^{max}, i \in N \tag{7}$$

Upper and lower bounds on the transformers tap ratios:

$$T_i^{min} \le T_i \le T_i^{max} , i \in N_T$$
 (8)

Upper and lower bounds on the compensators reactive powers:

$$Q_c^{min} \le Q_c \le Q_c^{max}, i \in N_C \tag{9}$$

Where N is the total number of buses,  $N_T$  is the total number of Transformers;  $N_c$  is the total number of shunt reactive compensators.

# 3. Flower Pollination Algorithm

Generally we use the following systems in Flower Pollination Algorithm (FPA),

- System 1. Biotic and cross-pollination has been treated as global pollination process, and pollen-carrying pollinators travel in a way which obeys Levy flights.
- System 2. For local pollination, A- biotic and self-pollination has been utilized.
- System 3. Pollinators such as insects can develop flower reliability, which is equivalent to a reproduction probability and it is proportional to the similarity of two flowers implicated.
- System 4. The communication of local pollination and global pollination can be controlled by a control probability  $p \in [0, 1]$ , with a slight bias towards local pollination.

System 1 and flower reliability can be represented mathematically as

$$x_i^{t+1} = x_i^t + \gamma L(\lambda)(x_i^t - g_*) \tag{10}$$

Where  $x_i^t$  is the pollen i or solution vector  $x_i$  at iteration t, and  $g_*$  is the current best solution found among all solutions at the current generation/iteration. Here  $\gamma$  is a scaling factor to control the step size.  $L(\lambda)$  is the parameter that corresponds to the strength of the pollination, which essentially is

also the step size. Since insects may move over a long distance with various distance steps, we can use a Levy flight to mimic this characteristic efficiently. We draw L > 0 from a Levy distribution

$$L \sim \frac{\lambda \Gamma(\lambda \sin(\Pi \lambda/2))}{\Pi} \frac{1}{s^{1+\lambda}} , (s \gg s_0 > 0)$$
 (11)

Here,  $\Gamma(\lambda)$  is the standard gamma function, and this distribution is valid for large steps s > 0. Then, to model the local pollination, for both system 2 and system 3 can be represented as

$$x_i^{t+1} = x_i^t + \in (x_i^t - x_k^t) \tag{12}$$

Where  $x_j^t$  and  $x_k^t$  are pollen from different flowers of the same plant species. This essentially mimics the flower reliability in a limited neighbourhood. Mathematically, if  $x_j^t$  and  $x_k^t$  comes from the same species or selected from the same population, this equivalently becomes a local random walk if we draw  $\in$  from a uniform distribution in [0,1]. Though Flower pollination performance can occur at all balance, local and global, neighbouring flower patch or flowers in the not-so-far-away neighbourhood are more likely to be pollinated by local flower pollen than those far away. In order to mimic this, we can effectively use a control probability (system 4) or proximity probability p to switch between common global pollination to intensive local pollination. To start with, we can use a raw value of p = 0.8 as an initially value.

The simplest method is to use a weighted sum to combine all multiple objectives into a composite single objective

$$f = \sum_{i=1}^{m} w_i f_i \sum_{i=1}^{m} w_i = 1 , w_i > 0$$
 (13)

Where m is the number of objectives and  $w_i(i = 1, ..., m)$  are non-negative weights.

FP Algorithm for solving optimal reactive power optimization

```
Step 1. Objective min of (x), x = (x_1, x_2, ..., x_d)
```

Step 2. Initialize a population of n flowers

Step 3. Find the best solution  $g_*$  in the initial population

Step 4. Define a control probability  $p \in [0, 1]$ 

Step5. Define a stopping criterion (a fixed number of generations/iterations)

Step6. while (t < Max Generation)

Step6. for i = 1: n (all n flowers in the population)

Step7. if rand < p,

Step8. Draw a (d-dimensional) step vector L which obeys a Levy distribution Global pollination through  $x_i^{t+1} = x_i^t + L(x_i^t - g_*)$ 

else

step9. Draw  $\in$  from a uniform distribution in [0,1]

step 10. Do local pollination through  $x_i^{t+1} = x_i^t + \in (x_i^t - x_k^t)$ 

end if

step10. Evaluate new solutions

step11. If new solutions are better, update them in the population

[Lenin \*, Vol.6 (Iss.8): August 2018] ISSN- 2350-0530(O), ISSN- 2394-3629(P) (Received: July 12, 2018 - Accepted: August 23, 2018) DOI: 10.5281/zenodo.1403795

end for

step 12. Find the current best solution  $g_*$  end while

Output - best solution has been found

# 4. Chaotic Maps

Chaos is a random state found in the non-linear dynamical deterministic system, possesses non-period, non-converging and bounded properties. The use of chaotic sequences is more beneficial than the random sequences due to its non-repetition and ergodicity properties. Borrowing the advantages of ergodicity, non-repetition and randomness of the chaotic sequences, the chaotic map is replacing the random sequences in generating the initial population in the FPA in this study. This is to ensure that the diversity of the initial population can be improved, where the distribution of the initial population is more uniform. Ten different chaotic maps are and circle map is selected for the integration with FPA.

$$x_{n+1} = \left(x_n + 0.2 - \left(\frac{0.5}{2\pi}\right)\sin(2\pi x_n)\right) \times mod(1)$$
 (14)

# 5. Shuffled Frog Leaping Algorithm

Shuffled frog leaping algorithm is a biological evolution algorithm based on swarm intelligence. The algorithm simulates a group of frogs in the wetland passing thought and foraging by classification of ethnic groups. In the execution of the algorithm, F frogs are generated at first to form a group, for N-dimensional optimization problem, frog i of the group is represented as  $X_i = (x_i^1, x_i^2, ..., x_i^N)$  then individual frogs in the group are sorted in descending order according to fitness values, to find the global best solution  $P_x$ . The group is divided into m ethnic groups, each ethnic group including n frogs, satisfying the relation  $F = m \times n$ . The rule of ethnic group division is: the first frog into the first sub-group, the second frog into the second sub-group, frog m into sub-group m, frog m + 1 into the first sub-group again, frog m + 2 into the second sub-group, and so on, until all the frogs are divided, then find the best frog in each sub-group, denoted by  $P_b$ ; get a worst frog correspondingly, denoted by  $P_w$ . Its iterative formula can be expressed as:

$$D = rand() * (P_b - P_\omega)$$
 (15)

$$P_{new_{-}\omega} = P_{\omega} + D_{i}, -D_{max} \le D_{i} \le D_{max}$$

$$(16)$$

Where rand () represents a random number between 0 and 1,

P<sub>b</sub> represents the position of the best frog,

P<sub>w</sub> represents the position of the worst frog,

D represents the distance moved by the worst frog,

 $P_{new_--\omega}$  is the improved position of the frog,

D<sub>max</sub> represents the step length of frog leaping.

In the execution of the algorithm, if the updated  $P_{new_--\omega}$  is in the feasible solution space, calculate the corresponding fitness value of  $P_{new_--\omega}$ , if the corresponding fitness value of  $P_{new_--\omega}$  is worse

than the corresponding fitness value of  $P_w$ , then use  $P_w$  to replace  $P_b$  in equation (15) and reupdate  $P_{new-\omega}$ ; if there is still no improvement, then randomly generate a new frog to replace  $P_w$ ;

repeat the update process until satisfying stop conditions.

## 6. Levy Flight

Levy flight is a rank of non-Gaussian random processes whose arbitrary walks are drawn from Levy stable distribution. This allocation is a simple power-law formula  $L(s) \sim |s|^{-1-\beta}$  where  $0 < \beta < 2$  is an index. Mathematically exclamation, a easy version of Levy distribution can be defined as,

$$L(s, \gamma, \mu) = \begin{cases} \sqrt{\frac{\gamma}{2\pi}} & exp\left[-\frac{\gamma}{2(s-\mu)}\right] \frac{1}{(s-\mu)^{3/2}} & if \ 0 < \mu < s < \infty \end{cases}$$
 (17)

Where  $\gamma > 0$  parameter is scale (controls the scale of distribution) parameter,  $\mu$  parameter is location or shift parameter. In general, Levy distribution should be defined in terms of Fourier transform

$$F(k) = \exp\left[-\alpha |k|^{\beta}\right], 0 < \beta \le 2,\tag{18}$$

Where  $\alpha$  is a parameter within [-1,1] interval and known as scale factor. An index of o stability  $\beta \in [0, 2]$  is also referred to as Levy index. In particular, for  $\beta = 1$ , the integral can be carried out analytically and is known as the Cauchy probability distribution. One more special case when  $\beta = 2$ , the distribution correspond to Gaussian distribution.  $\beta$  and  $\alpha$  parameters take a key part in determination of the distribution. The parameter  $\beta$  controls the silhouette of the probability distribution in such a way that one can acquire different shapes of probability distribution, especially in the tail region depending on the parameter  $\beta$ . Thus, the smaller  $\beta$  parameter causes the distribution to make longer jumps since there will be longer tail. It makes longer jumps for smaller values whereas it makes shorter jumps for bigger values. By Levy flight, new-fangled state of the particle is designed as,

$$X^{t+1} = X^t + \alpha \oplus Levy(\beta) \tag{19}$$

 $\alpha$  is the step size which must be related to the scales of the problem of interest. In the proposed method  $\alpha$  is random number for all dimensions of particles.

$$X^{t+1} = X^t + random\left(size(D)\right) \oplus Levy(\beta) \tag{20}$$

The product  $\bigoplus$  means entry-wise multiplications.

A non-trivial scheme of generating step size s samples are summarized as follows,

$$X^{t+1} = X^t + random\left(size(D)\right) \oplus Levy(\beta) \sim 0.01 \frac{u}{|v|^{1/\beta}} \left(x_j^t - gb\right)$$
 (21)

Where *u* and *v* are drawn from normal distributions. That is

[Lenin \*, Vol.6 (Iss.8): August 2018] ISSN- 2350-0530(O), ISSN- 2394-3629(P) (Received: July 12, 2018 - Accepted: August 23, 2018) DOI: 10.5281/zenodo.1403795

$$u \sim N(0, \sigma_v^2) \quad v \sim N(0, \sigma_v^2) \tag{22}$$

With

$$\sigma_{u} = \left\{ \frac{\Gamma(1+\beta)\sin(\pi\beta/2)}{\Gamma[(1+\beta)/2]\beta 2^{(\beta-1)/2}} \right\}^{1/\beta} , \sigma_{v} = 1$$
 (23)

Here  $\Gamma$  is standard Gamma function. One of the important points to be considered while performing distribution by Levy flights is the value taken by the  $\beta$  parameter and it substantially affects distribution.

# 7. Adapted Flower Pollination (AFP) algorithm

In the AFP algorithm, the initial population is generated using the circle map, frog leaping local search is performed by each solution and when rand>p, modified Levy flight with integration of inertia weight in global pollination is performed on that particular solution. The steps involved in the AFP are as follows:

# Step 1: Parameter Initialization

Initialize the relevant parameters of population size, n, dimension of search space, d, maximum iteration,  $max\_iter$ , switch probability, p, range of search space [Lb, Ubm], number of memeplexes, m and iterations within each memeplex, it.

Step 2: create Initial Population using the chaotic map

Step 3: Find the Best Solution

The fitness value of each solution is calculated and the best solution is determined.

Step 4: Perform the Frog Leaping Search - For each solution, search is performed.

Step 5: Perform the Global Search of Flower Pollination Algorithm

Step 6: Update the Solution

The fitness value of each new solution is evaluated. The historical position is updated through comparison with the new solution. Subsequently, the best solution is updated.

Step 7: Check Termination Condition or else, Step 4 is repeated.

## 8. Simulation results

Adapted Flower Pollination (AFP) algorithm has been tested in standard IEEE-57 bus power system. 18, 25 and 53 are reactive power compensation buses. PV buses are 2, 3, 6, 8, 9 and 12 and slack-bus is bus 1. In Table 1 system variable limits are given.

IEEE-57 preliminary conditions for the bus power system are given as follows:

$$P_{load} = 12.102 \text{ p.u. } Q_{load} = 3.020 \text{ p.u.}$$

Complete sum of initial generations and power losses are attained as follows:

$$\sum P_G = 12.410 \text{ p.u. } \sum Q_G = 3.3120 \text{ p.u.}$$

$$P_{loss} = 0.25841 \text{ p.u. } Q_{loss} = -1.2032 \text{ p.u.}$$

Control variables values obtained after optimization is given in Table 2. Comparisons of results are shown in Table 3.

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Table 1: Variable Limits

Table 1. Valiable Limits												
Reactive Power Generation Limits												
Bus no		1	2	2			6	8	9		12	
Qgminimum		-1.4	-1.401		02		-0.04	-1.3	-0.0	)3	-0.4	
Qgmaximum		1	0.3		0.4		0.21	1	0.04	1	1.50	
Voltage And Tap Setting Limits												
vgminimum	Vgmaximum		vpqminimum		n V	Vpqmaximum		tkminimum		tkmaximum		
0.9	1.0		0.91	0.91		1.05		0.9		1.0		
Shunt Capacitor Limits												
Bus no	18	2	5	53								
Qcminimum	0	0		0	•							
Qcmaximum	<b>1</b> 0	5	.2	6.1								

Table 2: Control variables obtained after optimization

List of Control AFP

List of Control	AFP			
Variables				
V1	1.100			
V2	1.03120			
V3	1.03110			
V6	1.02000			
V8	1.02000			
V9	1.00110			
V12	1.01010			
Qc18	0.06500			
Qc25	0.20010			
Qc53	0.04520			
T4-18	1.00020			
T21-20	1.04110			
T24-25	0.86010			
T24-26	0.87000			
T7-29	1.05000			
T34-32	0.87090			
T11-41	1.01000			
T15-45	1.03000			
T14-46	0.91000			
T10-51	1.02000			
T13-49	1.06000			
T11-43	0.91000			
T40-56	0.90000			
T39-57	0.95000			
T9-55	0.95000			

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Table 3: Comparison results

S.No.	Optimization	Finest	Poorest	Average
	Algorithm	Solution	Solution	Solution
1	NLP (Chaohua Dai et al .,2009)	0.25902	0.30854	0.27858
2	CGA (Chaohua Dai et al .,2009)	0.25244	0.27507	0.26293
3	AGA (Chaohua Dai et al .,2009)	0.24564	0.26671	0.25127
4	PSO-w (Chaohua Dai et al .,2009)	0.24270	0.26152	0.24725
5	PSO-cf (Chaohua Dai et al .,2009)	0.24280	0.26032	0.24698
6	CLPSO (Chaohua Dai et al .,2009)	0.24515	0.24780	0.24673
7	SPSO-07 (Chaohua Dai et al .,2009)	0.24430	0.25457	0.24752
8	L-DE (Chaohua Dai et al .,2009)	0.27812	0.41909	0.33177
9	L-SACP-DE (Chaohua Dai et al	0.27915	0.36978	0.31032
	.,2009)			
10	L-SaDE (Chaohua Dai et al .,2009)	0.24267	0.24391	0.24311
11	SOA (Chaohua Dai et al .,2009)	0.24265	0.24280	0.24270
12	LM (Gomes et al .,1999)	0.2484	0.2922	0.2641
13	MBEP1 (Gomes et al .,1999)	0.2474	0.2848	0.2643
14	MBEP2 (Gomes et al .,1999)	0.2482	0.283	0.2592
15	BES100 (Gomes et al .,1999)	0.2438	0.263	0.2541
16	BES200 (Gomes et al .,1999)	0.3417	0.2486	0.2443
17	Proposed AFP	0.22001	0.23002	0.22200

## 9. Conclusion

Adapted Flower Pollination (AFP) algorithm has been effectively applied for solving reactive power problem. And it has been tested in standard 57 bus test system. Performance comparisons with well-known population-based algorithms give improved results. Adapted Flower Pollination (AFP) algorithm emerges to find good solutions when compared to that of other reported algorithms. The simulation results presented in previous section prove the capability of AFP approach to arrive at near to global optimal solution.

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